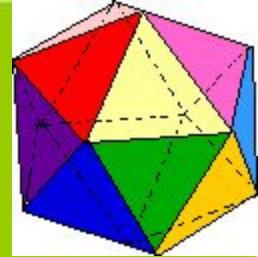
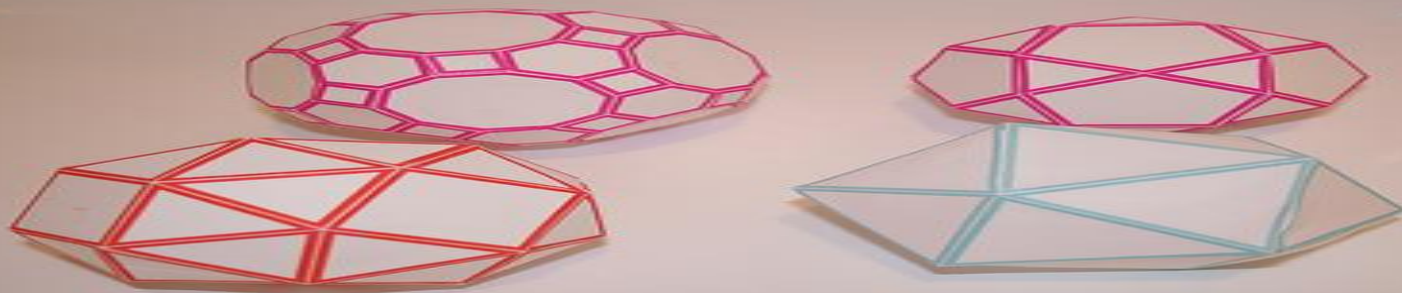


*'An order is to be observed in all things'*



# WELCOME





# A STUDY ON SEQUENCING MODELS

BY

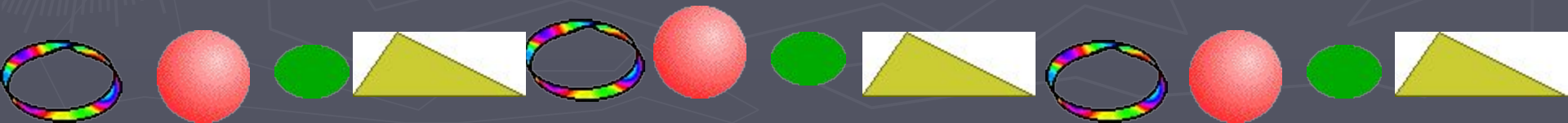
JYOTHY THOMAS

Assistant Professor

Department of Mathematics

Deva Matha College

Kuravilangad

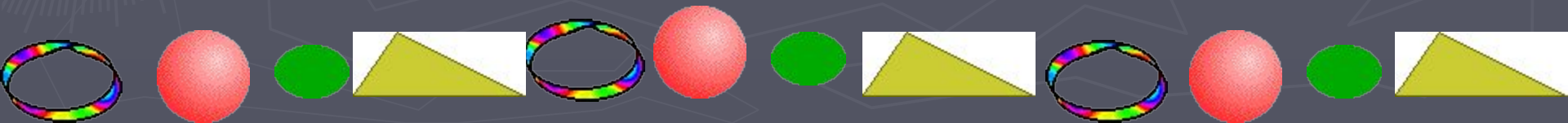


# SEQUENCING

**Definition:** Selection of an appropriate order for a series of job to be done on a number of service facilities so as to optimize the total effectiveness (may be time, cost etc which is a function of the order)

## BASIC TERMS

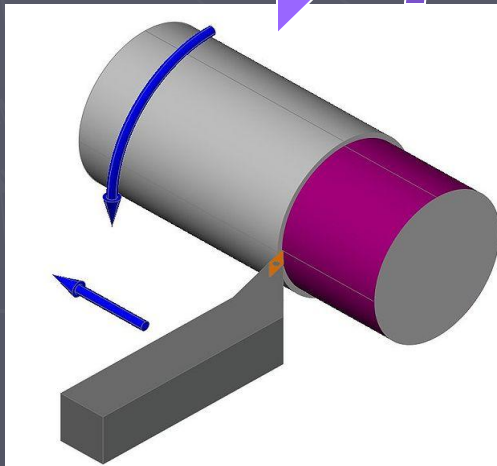
- ▶ Number of machines
- ▶ Processing order
- ▶ Processing time
- ▶ Idle time on a machine
- ▶ Total elapsed time
- ▶ No Passing Rule



# Machine operations in lathe

Materials 1, 2, 3, 4, 5,6 (Jobs)

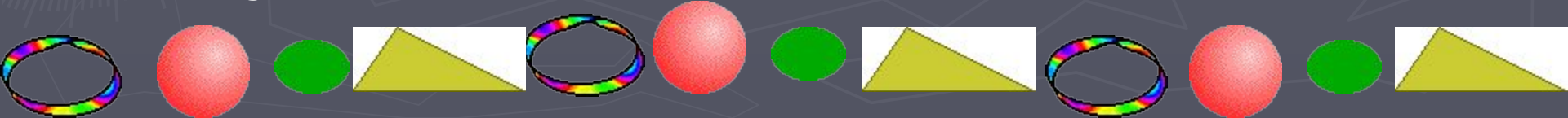
Job	1	2	3	4	5	6
Turning	3	12	5	2	9	11
Threading	8	6	4	6	3	1
Knurling	13	14	9	12	8	13



Turning

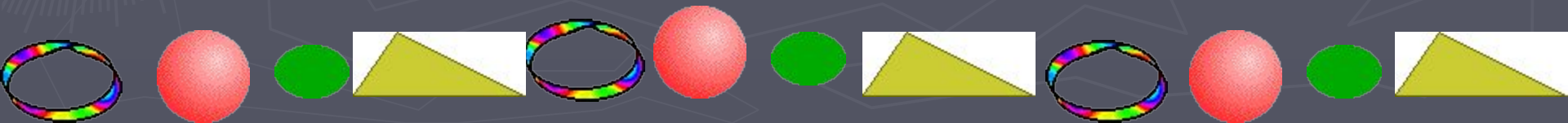
Threading

Knurling



# Machine operations in lathe

- ▶ Machine order fixed – Turning Threading Knurling
- ▶ Job order 123456 132456 . . . .  
234561 243561 . . . .  
345612 354612 . . . .  
456123 465123 . . . .  
561234 516234 . . . .  
612345 621345 . . . Total 6! Orders
- ▶ From these find the order which minimizes time/cost
- ▶ This is a 6 job – 3 machine problem



# Sequencing in computer systems

Programs 1, 2, 3, 4 (Jobs)

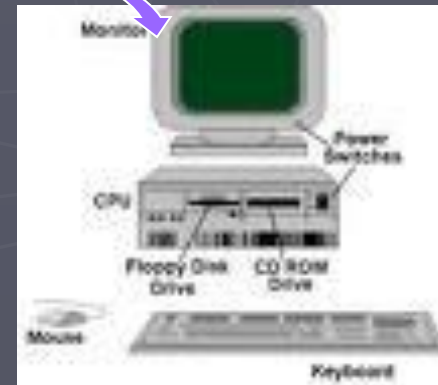
Job	1	2	3	4	5
M	3	8	7	5	2
CPU	3	4	2	1	5
I/O	5	8	10	7	6



Memory



CPU



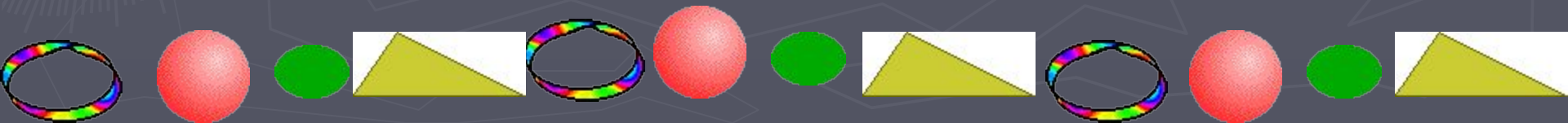
Input/ Output

This is a 4 job – 3 machine sequencing problem



# General Sequencing problem

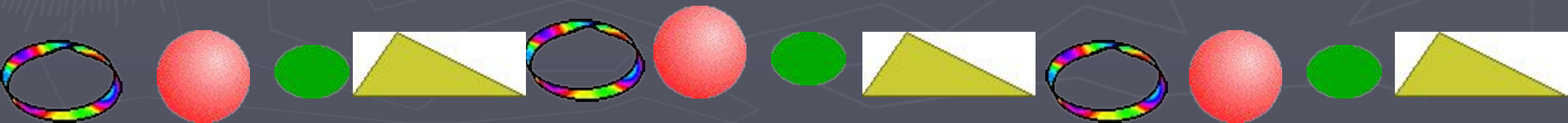
- ▶ n jobs on m machines
- ▶  $(n!)^m$  possible sequences
- ▶ Find the sequence minimizing the total time
- ▶ When  $n = 4$ ,  $m = 5$  there are  
 $(4!)^5 = 7962624$  possible sequences
- ▶ Enumeration impossible for even smaller m and n



# Processing n jobs through 2 machines

## General Form

Jobs	1	2	...	n
Mac A	$a_1$	$a_2$	...	$a_n$
Mac B	$b_1$	$b_2$	...	$b_n$

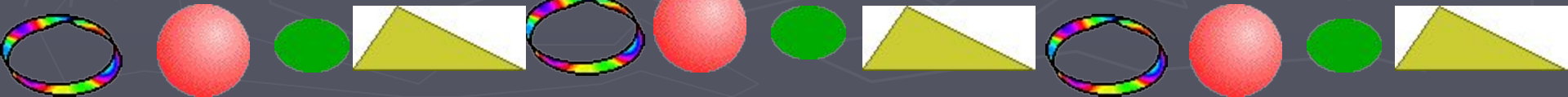
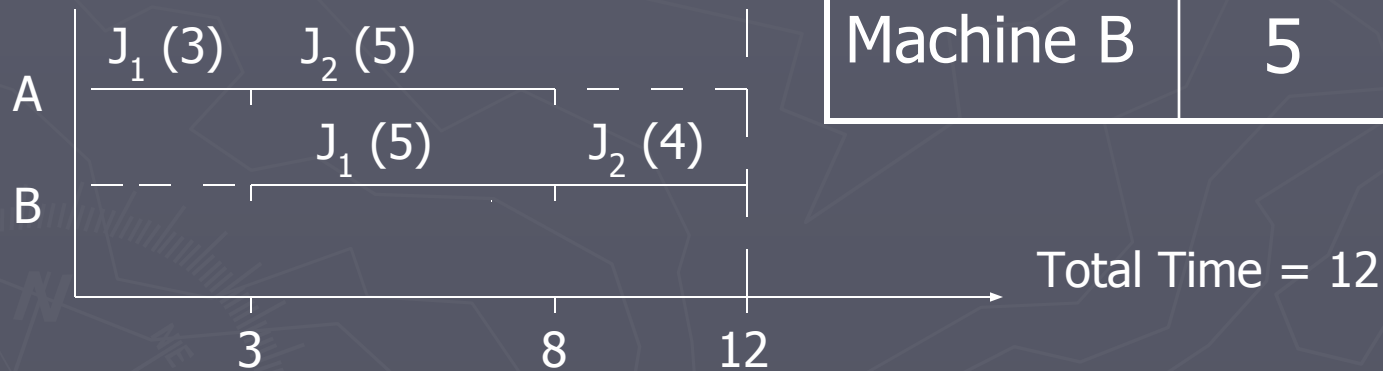




# Gnatt Chart

- Consider the two job - Two machine problem

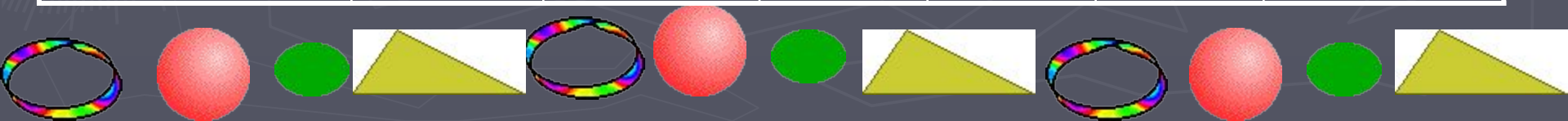
Job	J <sub>1</sub>	J <sub>2</sub>
Machine A	3	5
Machine B	5	4



# Optimum Sequence Algorithm

*Illustration:* A book binder has a printing press, a binding machine & the manuscripts of different books. The processing times are given. Determine the optimum sequence.

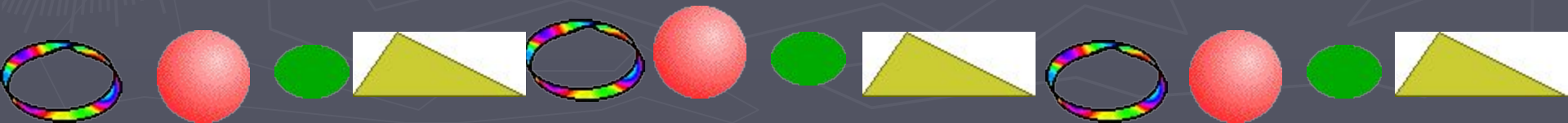
BOOK	1	2	3	4	5	6
Printing Time (hrs)	30	120	50	20	90	100
Binding Time (hrs)	80	100	90	60	30	10



# Optimum sequence Algorithm

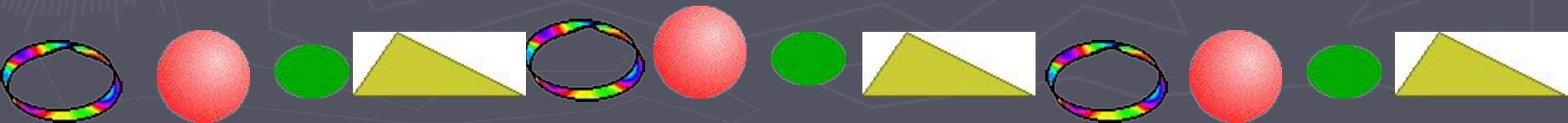
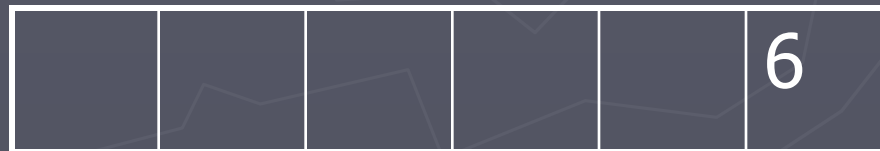
► Find the smallest processing time. If it is for first machine, place the job in first available position of the sequence. If it is for second machine place the job in the last available position of the sequence.

► If there is a tie



# Optimum sequence Algorithm

- (i) among the two machines ( $a_k = b_r$ ) place job corresponding to first machine (job k) in first available position of the sequence and the job corresponding to second machine (job r) in the last available position of the sequence.
- (ii) among same machine ( $a_k = a_r / b_k = b_r$ ), break the tie arbitrarily



# Optimum sequence Algorithm

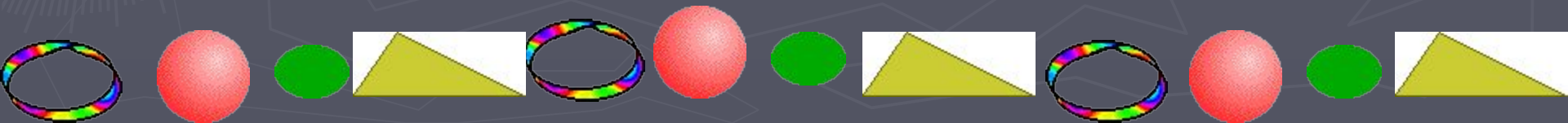
- ▶ Cross off the jobs already assigned and repeat the above procedure

4					6
---	--	--	--	--	---

4	1			5	6
---	---	--	--	---	---

4	1	3		5	6
---	---	---	--	---	---

4	1	3	2	5	6
---	---	---	---	---	---



# Optimum sequence Algorithm

- Calculate the idle times and total elapsed time

Books	Printing		Binding		Idle times	
	In	Out	In	Out	Printing	Binding
4	0	20	20	80	0	20
1	20	50	80	160	0	0
3	50	100	160	250	0	0
2	100	220	250	350	0	0
5	220	310	350	380	0	0
6	310	410	410	420	10	30



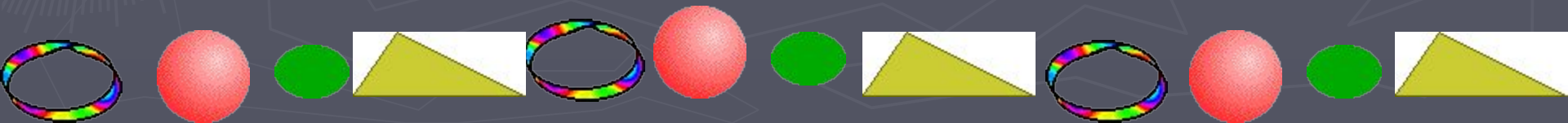
# Processing n jobs through 3 machines

## ► General form

Jobs	1	2	...	n
Mac A	$a_1$	$a_2$	...	$a_n$
Mac B	$b_1$	$b_2$	...	$b_n$
Mac C	$c_1$	$c_2$	...	$c_n$

## ► Solution Procedure

If minimum among  $a_i$  / among  $c_i$  is greater than or equal to the maximum among  $c_i$  then we can reduce this to an n job – 2 machine problem as below:

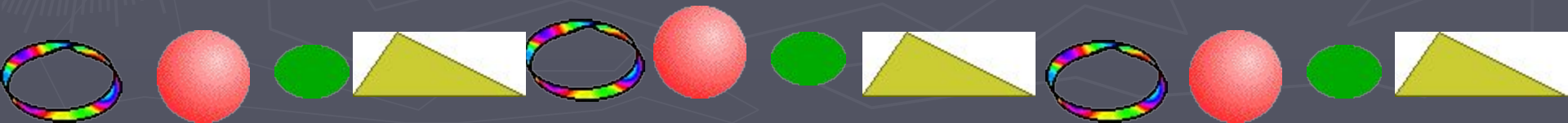


# Processing n jobs through 3 machines

Introduce two fictitious machines G and H whose processing times are defined by

$$g_i = a_i + b_i \quad \& \quad h_i = b_i + c_i$$

Then proceed as in the above case





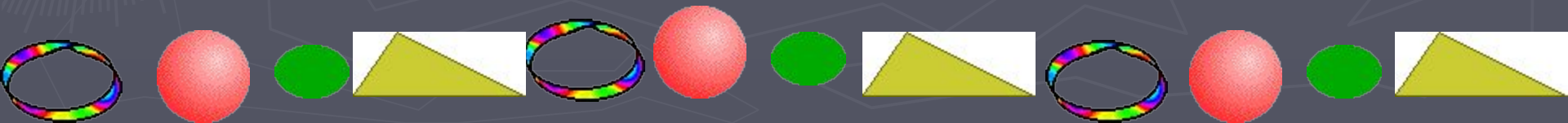
# Processing n jobs through m machines

## ► General form

Jobs	1	2	...	n
Mac A	$a_1$	$a_2$	...	$a_n$
Mac B	$b_1$	$b_2$	...	$b_n$
...	...	...	...	...
Mac F	$f_1$	$f_2$	...	$f_n$

## ► Solution Procedure

If minimum among  $a_i$  / among  $f_i$  is greater than or equal to the maximum among  $b_i, c_i, \dots, e_i$  then we can reduce this to an n job – 2 machine problem as below



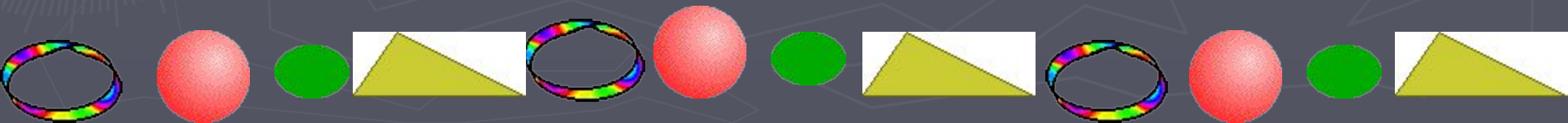
# Processing n jobs through m machines

Introduce two fictitious machines G and H whose processing times are defined by

$$g_i = a_i + b_i + \dots + e_i \quad \&$$

$$h_i = b_i + c_i + \dots + f_i$$

Then proceed as in the above case

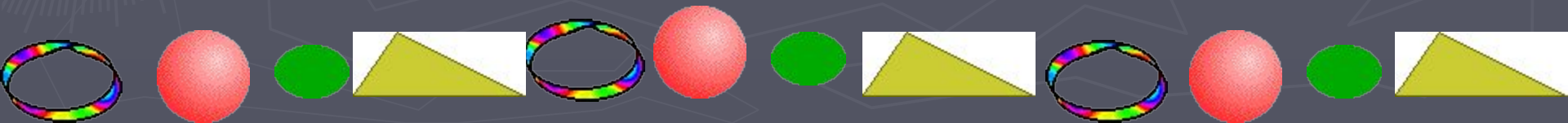


# EXAMPLE

- Determine the optimum sequence for the 4 job – 6 machine problem.

Machines	$M_1$	$M_2$	$M_3$	$M_4$	$M_5$	$M_6$
Job A	18	8	7	2	10	25
Job B	17	6	9	6	8	19
Job C	11	5	8	5	7	15
Job D	20	4	3	4	8	12

Min of  $M_1 = 11$ , Max  $M_2, M_3, M_4, M_5 = 10$ , Min  $M_6 = 12$

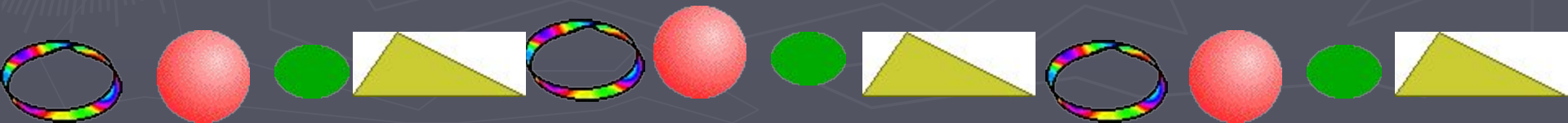


# Solution

Condition for fictitious Machines is satisfied.

Jobs		A	B	C	D
Fictitious	Machine G	45	46	36	39
	Machine H	52	48	40	31

Sequence



# Processing

Jobs	$M_1$		$M_2$		$M_3$		$M_4$		$M_5$		$M_6$	
	In	Out	In	Out	In	Out	In	Out	In	Out	In	Out
C	0	-11	11	-16	16	-24	24	-29	29	-36	36	-51
A	11	-29	29	-37	37	-44	44	-46	46	-56	56	-81
B	29	-46	46	-52	52	-61	61	-67	67	-75	81	-100
D	46	-66	66	-70	70	-73	73	-77	77	-85	100	-112

Total elapsed time = 112 hrs

Idle times  $M_1$  to  $M_6$  are 46, 89, 85, 95, 79, 41 respectively

